

I Claim:

- 1        1. A method for determining the state of stability of an electrical grid having n nodes,  
2 comprising the steps of:
  - 3            a. embedding load flow equations ( $L$ ) representing the electrical grid in a parametric  
4 homotopy ( $L(s)$ ) that goes continuously from a 0-case ( $L(0)$ ), in which all voltages are equal to  
5 the nominal voltage and there is no energy flow in links of the grid, to an objective case ( $L(1)$ )  
6 representative of the grid in the condition for which stability is to be determined;
  - 7            b. developing in power series values of the load flow equations' unknowns in the  
8 parameters of the parametric homotopy ( $L(s)$ ) in a neighborhood of the 0-case value of each  
9 parameter;
  - 10          c. computing a continued fraction approximation to the power series coefficients  
11 produced in step b;
  - 12          d. evaluating the n-order approximant of the continued fraction approximation produced  
13 in step c for the power series coefficients produced in step b to provide a solution to the load  
14 flow equations ( $L$ ); and
  - 15          e. displaying the solution to the load flow equations as a measure of the state of stability  
16 of the electrical grid.

- 1        2. The method of claim 1, further comprising the steps of:
  - 2            prior to said embedding step, receiving data from a supervisory and data acquisition  
3 system representative of conditions of the electrical grid, and forming said load flow equations  
4 ( $L$ ) from said data.

1           3. The method of claim 2, further comprising the steps of repeating said receiving step  
2       and steps a through e continuously to provide a continuous, real time estimation of the stability  
3       of the electrical grid.

1           4. The method of claim 3, further comprising the steps of confirming that a set of  
2       voltages and flows contained in said solution to said load flow equations (L) are representative of  
3       a physical electrical state.

1           5. A method of measuring load flow in a power generating system having an electrical  
2       grid comprised of n nodes, comprising the steps of:

3           a. embedding load flow equations (L) representing the electrical grid in a parametric  
4       homotopy (L(s)) that goes continuously from a 0-case (L(0)), in which all voltages are equal to  
5       the nominal voltage and there is no energy flow in links of the grid, to an objective case (L(1))  
6       representative of the grid in the condition for which stability is to be determined;

7           b. developing in power series values of the load flow equations' unknowns in the  
8       parameters of the parametric homotopy (L(s)) in a neighborhood of the 0-case value of each  
9       parameter;

10          c. computing a continued fraction approximation to the power series coefficients  
11       produced in step b;

12          d. evaluating the n-order approximant of the continued fraction approximation produced  
13       in step c for the power series coefficients produced in step b to provide a solution to the load  
14       flow equations (L); and

15           e. displaying the solution to the load flow equations as a measure of the load flow in the  
16       power generating system.

1           6. The method of claim 5, further comprising the steps of:

2           prior to said embedding step, receiving data from a supervisory and data acquisition  
3       system representative of conditions of the electrical grid, and forming said load flow equations  
4       (L) from said data.

1           7. The method of claim 6, further comprising the steps of repeating said receiving step  
2       and steps a through e continuously to provide a continuous, real time measure of the load flow in  
3       the power generating system.

1           8. A method of measuring load flow in a power generating system having an electrical  
2       grid, comprising the steps of:

3           a. generating a mathematical model of a known, physical solution to the load flow  
4       equations (L) in which all voltages are equal to the nominal voltage and there is no energy flow  
5       in links of the grid;

6           b. using analytical continuation to develop a mathematical model of the current, physical  
7       solution to the load flow equations representing the current load flow in the power generating  
8       system; and

9           c. displaying the physical solution to the load flow equations as a measure of the load  
10      flow in the power generating system.

1           9. The method of claim 8, said generating step further comprising developing a power  
2 series expansion of all quantities in a parametric homotopy ( $L(s)$ ) formed from said load flow  
3 equations ( $L$ ) in a neighborhood of the 0-case value of each quantity.

1           10. The method of claim 9, further comprising using algebraic approximants to  
2 determine the sum of all coefficients of said power series for the load flow equations  
3 representative of the physical current load flow that is to be determined.

1           11. A system for measuring load flow in a power generating system having an electrical  
2 grid, said system comprising:

3           a supervisory control and data acquisition system adapted to collect data from said  
4 electrical grid indicative of electrical conditions in said electrical grid, said supervisory control  
5 and data acquisition system being in communication with a microprocessor-controlled energy  
6 management system, said energy management system further comprising executable computer  
7 instructions to:

8           a. process said data received from said supervisory control and data acquisition  
9 system into load flow equations ( $L$ ) representing the electrical grid;

10           b. embed said load flow equations ( $L$ ) in a parametric homotopy ( $L(s)$ ) that goes  
11 continuously from a 0-case ( $L(0)$ ), in which all voltage are equal to the nominal voltage and  
12 there is no energy flow in links of the grid, to an objective case ( $L(1)$ ) representative of the grid  
13 in the condition for which stability is to be determined;

- 14                   c. develop in power series values of the load flow equations' unknowns in the  
15       parameters of the parametric homotopy ( $L(s)$ ) in a neighborhood of the 0-case value of each  
16       parameter;
- 17                   d. compute a continued fraction approximation to the power series coefficients  
18       produced in step c;
- 19                   e. evaluate the n-order approximant of the continued fraction approximation  
20       produced in step d for the power series coefficients produced in step c to provide a solution to the  
21       load flow equations ( $L$ ); and
- 22                   f. display the solution to the load flow equations as a measure of the state of  
23       stability of the electrical grid.